

# Simplifying Radicals Primer

Rules:  $\sqrt{ab} = \sqrt{a} \cdot \sqrt{b}$   $a \geq 0$   
 $b \geq 0$  \* cannot have a  
 $\sqrt{\frac{a}{b}} = \frac{\sqrt{a}}{\sqrt{b}}$   $a \geq 0$   
 $b > 0$  RADICAL in the  
denominator of a fraction

$$\sqrt{a} \cdot \sqrt{a} = (\sqrt{a})^2 = a$$

$$M\sqrt{a} \cdot N\sqrt{b} = MN\sqrt{ab} \quad a, b \geq 0$$

egs: SIMPLIFY the following:

a)  $\sqrt{25} = \boxed{5}$

b)  $\sqrt{24} = \sqrt{4 \cdot 6} = \sqrt{4} \cdot \sqrt{6} = \boxed{2\sqrt{6}}$

c)  $\sqrt{125} = \sqrt{25 \cdot 5} = \sqrt{25} \cdot \sqrt{5}$   
 $= \boxed{5\sqrt{5}}$

d)  $\frac{\sqrt{48}}{\sqrt{6}} = \sqrt{\frac{48}{6}} = \sqrt{8}$   
 $= \boxed{2\sqrt{2}}$

e)  $\sqrt{\frac{2}{9}} = \frac{\sqrt{2}}{\sqrt{9}} = \boxed{\frac{\sqrt{2}}{3}}$

f)  $\frac{3\sqrt{5} + 12}{6} = \frac{3\sqrt{5}}{6} + \frac{12}{6}$   
 $= \boxed{\frac{\sqrt{5}}{2} + 2}$

g)  $\frac{3\sqrt{18} - 27}{9} = \frac{9\sqrt{2} - 27}{9}$   
 $= \frac{9\sqrt{2}}{9} - \frac{27}{9}$   
 $= \boxed{\sqrt{2} - 3}$

h)  $\frac{2\sqrt{3} \cdot 5\sqrt{8}}{10\sqrt{6}}$   
 $= \frac{10\sqrt{24}}{10\sqrt{6}} = \sqrt{4} = 2$

$$h) \frac{1}{\sqrt{2}} = \frac{1}{\sqrt{2}} \cdot \frac{\sqrt{2}}{\sqrt{2}} = \boxed{\frac{\sqrt{2}}{2}}$$

$$i) \sqrt{\frac{28}{3}} = \frac{\sqrt{28}}{\sqrt{3}} = \frac{2\sqrt{7}}{\sqrt{3}} \cdot \frac{\sqrt{3}}{\sqrt{3}} = \boxed{\frac{2\sqrt{21}}{3}}$$

hvk: Worksheet

## Ch. 4.1 - Solving Quadratics (a=1) by Factoring

When you multiply two binomials (using FOIL), the result may be generalized as follows:

$$\begin{array}{cc} (x+m) & (x+n) \\ \hline 2 & 3 \\ \hline \end{array} \begin{array}{cc} (x+n) & \\ \hline 2 & 4 \\ \hline \end{array} = x^2 + mx + nx + mn$$
$$= x^2 + (m+n)x + mn$$

This shows that:

a QUADRATIC (degree 2) expression

- (i) The product of two binomials is a TRINOMIAL.
- (ii) The first term,  $x^2$ , is a product of  $x \cdot x$ .
- (iii) The middle term's coefficient is the sum of  $m \neq n$ .
- (iv) The last term is a product of  $m \neq n$ .

Generalized trinomial  $\Rightarrow \underline{ax^2 + bx + c}$ , but  
when  $a=1$ ,  $\underline{x^2 + bx + c}$

(always arrange in descending order of powers).

FOUR TYPES:

- (1)  $x^2 + bx + c = (x + \underline{\quad})(x + \underline{\quad})$
- (2)  $x^2 - bx + c = (x - \underline{\quad})(x - \underline{\quad})$
- (3)  $x^2 + bx - c = (x + \underline{\quad})(x - \underline{\quad})$  bigger number  $\oplus$
- (4)  $x^2 - bx - c = (x + \underline{\quad})(x - \underline{\quad})$  smaller number  $\oplus$

eg1: Factor the following:

a)  $x^2 + 7x + 12$

$$\frac{x}{12} \pm \frac{7}{7} = (x+4)(x+3)$$

4, 3

b)  $x^2 - 7x + 6$

$$\frac{x}{6} \pm \frac{-7}{-7} = (x-6)(x-1)$$

-6, -1

c)  $x^2 + 3x - 10$

$$\frac{x}{-10} \pm \frac{3}{-2} = (x-2)(x+5)$$

-2, 5

d)  $x^2 - 2x - 8$

$$\frac{x}{-8} \pm \frac{-2}{-2} = (x-4)(x+2)$$

-4, 2

e)  $x^2 + 8 - 6x$

$$\frac{x}{8} \pm \frac{-6}{-4} = x^2 - 6x + 8 = (x-4)(x-2)$$

-4, -2

f)  $x^2 - 2x + 4$

$$\frac{x}{4} \pm \frac{-2}{-2} \quad \underline{\text{UNFACTORABLE}}$$

g)  $x^2 + 4xy - 21y^2$

$$\frac{x}{-21} \pm \frac{4}{4} = (x+7y)(x-3y)$$

7, -3

h)  $5x^2 + 35x + 60$

$$= 5(x^2 + 7x + 12) = 5(x+4)(x+3)$$

4, 3

i)  $-x^2 + 5x + 6$

$$= -1(x^2 - 5x - 6)$$

$$\frac{x}{-6} \pm \frac{5}{-5} = -1(x-6)(x+1)$$

-6, 1

j)  $-3x^4 - 18x^3 - 27x^2$

$$= -3x^2(x^2 + 6x + 9)$$

$$\frac{x}{9} \pm \frac{6}{6} = -3x^2(x+3)(x+3) = -3x^2(x+3)^2$$

# Factoring Difference of Squares $(a^2x^2 - b^2y^2)$ ; $a \neq 0$ $b \neq 0$

Rule:  $a^2 - b^2 = (a+b)(a-b)$

eg 2: Factor the following

a)  $x^2 - 16$   
 $= (x+4)(x-4)$

b)  $x^4 - 4y^2$   
 $= (x^2 - 2y)(x^2 + 2y)$

c)  $x^4 - 16$   
 $= (x^2 + 4)(x^2 - 4)$   
 $= (x^2 + 4)(x+2)(x-2)$

d)  $16x^2 - 4$   
 $= (4x+2)(4x-2)$

e)  $(x^2 - 6x + 9)^{\text{typo}} - y^2$   
 $= (x-3)(x-3) - y^2$   
 $= (x-3)^2 - y^2$   
 $= ((x-3)+y)((x-3)-y)$

f)  $(16x^2 + 24xy + 9y^2) - (4a^2 - 4ab + b^2)$   
 $= (4x+3y)(4x+3y) - (2a+b)(2a+b)$   
 $= (4x+3y)^2 - (2a+b)^2$   
 $= ((4x+3y)+(2a+b))((4x+3y)-(2a+b))$

p. 163 - 168 # 1-14.  
(omit ~~9~~ 13ef, 14 c-f)

Ch. 4.2 - Factoring trinomials where  $a \neq 1$   
( $ax^2 + bx + c$ )

... and ... where 'a' cannot be factored out!

\* if you'd like, read the book's methods on  
p. 169 and p. 171  $\Rightarrow$  perfectly acceptable methods.

Best method? Factoring by DECOMPOSITION.

$\hookrightarrow$  not in book.

- Steps:
- ① Find two numbers that multiply to give (ac) and add to give b.
  - ② Rewrite "middle term" (bx) as a sum of the two numbers (ie. make the trinomial a 'tetranomial').
  - ③ Factor in groups of two.
  - ④ Factor out the common binomial.

eg!: Factor  $2x^2 + 7x - 4$

	$\frac{x}{-8}$	$\frac{+}{7}$
	8,	-1

$$= (2x^2 + 8x)(-1x - 4)$$
$$= 2x(x+4) - 1(x+4)$$
$$= \boxed{(x+4)(2x-1)}$$

eg2: Factor  $12x^2 - 5x - 2$

$\frac{x}{-24}$	$\frac{+}{-5}$
	$-8, 3$

$$= 12x^2 - 8x + 3x - 2$$

$$= 4x(3x-2) + 1(3x-2)$$

$$= (3x-2)(4x+1)$$

eg3: Factor  $-10x^3 + 2x^2 + 12x$

\* 1st: factor to create QUADRATIC expression

$$= -2x(5x^2 - 1x - 6)$$

FACTOR this by decomposition

$\frac{x}{-30}$	$\frac{+}{-1}$
	$-6, 5$

$$= -2x(5x^2 + 5x - 6x - 6)$$

$$= (-2x)(5x)(x+1) - 6(x+1)$$

$$= -2x(x+1)(5x-6)$$

Def'n: A trinomial that is a square of a binomial is called a PERFECT SQUARE TRINOMIAL.

For  $ax^2 + bx + c$  to be a perfect sq. trinomial:

- i)  $c$  must be positive, and a perfect square
- ii)  $a$  must be a perfect square
- iii)  $b$  is the sq.rt. of  $ax^2$ , multiplied by the sq.rt. of  $c$ , then doubled. (could be  $\oplus$  or  $\ominus$ ).

eq 4: Factor:

a)  $x^2 + 8x + 16$

$$= (x+4)(x+4)$$

$$= \boxed{(x+4)^2}$$

b)  $4x^2 - 12x + 9$

$$= (2x-3)(2x-3)$$

$$= (2x-3)^2$$

or just use DECOMP.

c)  $(x-2y)^2 - 2(x-2y) + 1$

$$= ((x-2y)-1)((x-2y)-1)$$

$$= \boxed{((x-2y)-1)^2}$$

eq 5 Find all integers  $k$  such that each trinomial is a perfect square:

a)  $x^2 + 6x + k$

$$3+3=6$$

$$3 \times 3 = \boxed{k=9}$$

b)  $9x^2 - kx + 4$

$$\sqrt{9} = 3$$

$$\sqrt{4} = 2$$

$$3 \times 2 = 6$$

$$k = 6 + 6 = \boxed{12}$$

$$k = -6 + -6 = \boxed{-12}$$

c)  $kx^2 + 12x + 9$

$$\sqrt{9} = 3$$

$$\frac{12}{2} = 6$$

$$3 \times ? = 6$$

$$? = 2$$

$$\sqrt{k} = 2$$

$$\boxed{k=4}$$

P. 173-176  
#1-8

+ QUIZ

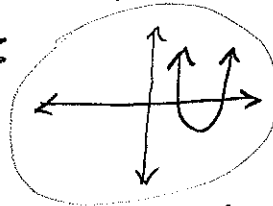
omit 8 3] 6d

2l typo!

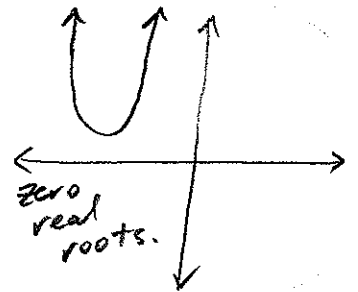
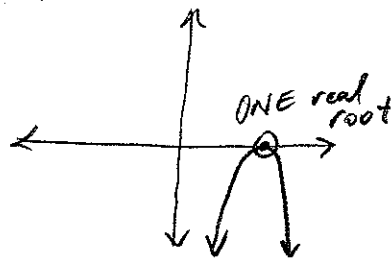
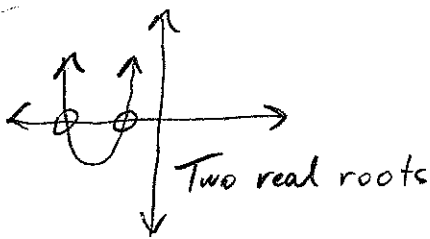


# Ch. 6.1 - Solving Quadratic Equations by Factoring

When graphed, a quadratic function ( $y = ax^2 + bx + c$ ) results in a PARABOLA:  $f(x) =$



When  $y=0$ , solving for  $x$  gives the x-intercepts (real zeros) (roots) of the function and there are three general possibilities:



A quadratic equation is written in the form

$$\boxed{ax^2 + bx + c = 0 \text{ where } a, b, c \in \mathbb{R} \text{ and } a \neq 0.}$$

GENERAL FORM

Again, solving for  $x$  finds the x-intercepts (real roots) (real zeros) of  $y = ax^2 + bx + c$

## Zero Factor Property

The equation  $mn = 0$  is true if either  $m = 0$  or  $n = 0$ .

eg! Solve by factoring:

$$\begin{array}{r} x \\ -6 \\ -3, 2 \end{array}$$

$$x^2 - x - 6 = 0$$

$$(x-3)(x+2) = 0$$

so... for this to be true, either  $(x-3) = 0$  and/or  $(x+2) = 0$

HINT: when  $x^2$ 's coefficient is 1, read constant of binomial as opposite

$$\boxed{x = 3}$$

$$\boxed{x = -2}$$

eg2: Solve by factoring:

$$2x^2 - 9x + 10 = 0$$

$$\frac{x}{20} \quad +$$

$$2x^2 - 4x - 5x + 10 = 0$$

$$-5, -4$$

$$2x(x-2) - 5(x-2) = 0$$

$$(x-2)(2x-5) = 0$$

$$x-2=0$$

$$\boxed{x=2}$$

$$2x-5=0$$

$$2x=5$$

$$\boxed{x=\frac{5}{2}}$$

Check

hint.

When  $ax-b=0$   
 $x=\frac{b}{a}$

eg3: Solve by factoring

$$3x^2 + 15x = 0$$

(ie: When  $c=0$ )

$$3x(x+5) = 0$$

$$3x=0$$

$$\boxed{x=0}$$

$$\boxed{x=-5}$$

So... when  $c=0$ , one solution will be  $\boxed{x=0}$

eg4: Solve by factoring

$$3x^2 - 7x = 20$$

$$3x^2 - 7x - 20 = 0$$

$$\frac{x}{-60} \quad +$$

$$3x^2 - 12x + 5x - 20 = 0$$

$$-12, 5$$

$$3x(x-4) + 5(x-4) = 0$$

$$(x-4)(3x+5) = 0$$

$$\boxed{x=4, -\frac{5}{3}}$$

eg 5: Solve by factoring:

$$\frac{x}{x-5} - \frac{3}{x+1} = \frac{30}{x^2-4x-5}$$

\* find common denominator!  
 $(x-5)(x+1) = x^2-4x-5$

$$\frac{x(x-5)(x+1)}{(x-5)} - \frac{(3)(x-5)(x+1)}{(x+1)} = \frac{30(x-5)(x+1)}{(x-5)(x+1)}$$

$$x(x+1) - 3(x-5) = 30$$

$$x^2 + x - 3x + 15 = 30$$

$$x^2 - 2x - 15 = 0$$

$$(x-5)(x+3) = 0$$

$$\boxed{x = \cancel{5}, -3}$$

eg 6: For each of the following, write a quadratic equation given the real roots:

a) 2, -5

$$(x-2)(x+5) = 0$$

$$\boxed{x^2 + 3x - 10 = 0}$$

b) 0, 6

$$x(x-6) = 0$$

$$\boxed{x^2 - 6x = 0}$$

c)  $\frac{2}{3}, -\frac{1}{2}$

$$(3x-2)(2x+1) = 0$$

$$\boxed{6x^2 - x - 2 = 0}$$

p 265-270: # 1-9 omit 3b+d omit 8e  
(word probs. <sup>(10-15)</sup> now, if you want, or later...)

# Ch. 6.2 - The Square Root Principle and

## Completing the Square

Square Root Principle - may be used when

$b=0$  in  $ax^2+bx+c=0$ . (becomes  $ax^2+c=0$ )

Possibilities: i) If  $\frac{-c}{a} > 0$ , there will be two solutions.

ii) If  $\frac{-c}{a} = 0$ , there will be one solution ( $x=0$ ).

iii) If  $\frac{-c}{a} < 0$ , there will be no real roots.

eg1: Solve the following using the sq. root principle:

a)  $x^2 - 4 = 0$

$$\sqrt{x^2} = \sqrt{4}$$

$$x = \pm\sqrt{4}$$

$$x = \pm 2$$

b)  $x^2 + 9 = 0$

$$\sqrt{x^2} = \sqrt{9}$$

c)  $\sqrt{(x-2)^2} = \sqrt{16}$  }  $x-2 = \pm 4$   
 $x-2 = \pm\sqrt{16}$  }  $x = 6, -2$

no solution!

eg2: Solve using the sq. root principle:

a)  $3x^2 - 8 = 0$

$$3x^2 = 8$$

$$\sqrt{x^2} = \sqrt{\frac{8}{3}}$$

$$x = \pm\sqrt{\frac{8}{3}}$$

$$x = \pm\frac{2\sqrt{6}}{3}$$

\*haven't  
learnt  
radicals  
yet!

b)  $(x-1)^2 = 12$

$$\sqrt{(x-1)^2} = \sqrt{12}$$

$$x-1 = \pm\sqrt{12}$$

$$x = \pm\sqrt{12} + 1$$

$$x = \pm 2\sqrt{3} + 1$$

$\Phi_s: 1, 2$   
p. 273

## Instructions for Completing the Square in order to solve Quadratic Equations

Typical Quadratic Equation:  $ax^2 + bx + c = 0$ ;  $a \neq 0$

Type I – When  $a = 1$

1. Write equation in  $x^2 + bx + c = 0$  form (in order of descending powers);
2. Move 'c' to the 'other' side (if 'c' is zero, don't do anything);
3. Calculate half of 'b' and write the number in a box;
4. Square the number in the box and write it in a circle beside the box;
5. Add the number in the circle to BOTH sides of the equation;
6. Complete the square! (ie. Turn the trinomial into a square of a binomial) –  
HINT: the binomial will *always* be  $x$  and the number in the box, all squared!
7. Use the square root principle to solve the equation.

Type II – When  $a \neq 1$

1. Write equation in a  $x^2 + bx + c = 0$  form (in order of descending powers);
2. Move 'c' to the 'other' side (if 'c' is zero, don't do anything);
3. Factor 'a' out of a  $x^2$  and  $bx$  (could create fractions – that's OK!) – this will create a "new" 'b' value;
4. Calculate half of the "new" 'b' value and write the number in a box;
5. Square the number in the box and write it in a circle beside the box;
6. A. Add the number in the circle in brackets on the variable side of the equation;  
B. Multiply the number you added in brackets by the 'a' value that you factored out and add the product to the 'other' (non-variable) side.
7. Complete the square! (ie. Turn the trinomial in to a square of a binomial) –  
HINT: the binomial will *always* be  $x$  and the number in the box, all squared!
8. Use the square root principle to solve the equation.

## Completing the Square

- can be utilized if quadratic cannot be factored.
- see instruction sheet.

eg1: Solve by Completing the Square

$$x^2 - 6x - 27 = 0 \quad \boxed{-3} \text{ } \textcircled{9}$$

$$x^2 - 6x = 27$$

$$x^2 - 6x + 9 = 27 + 9$$

$$\sqrt{(x-3)^2} = \sqrt{36}$$

$$x-3 = \pm 6$$

$$\boxed{x = 9, -3}$$

eg2:  $x^2 + 8x + 11 = 0$

$$x^2 + 8x = -11 \quad \boxed{+4} \text{ } \textcircled{16}$$

$$x^2 + 8x + 16 = -11 + 16$$

$$\sqrt{(x+4)^2} = \sqrt{5}$$

$$x+4 = \pm \sqrt{5}$$

$$\boxed{x = \pm \sqrt{5} - 4}$$

eg3: Solve  $-x^2 + 8x - 17 = 0$

$$x^2 - 8x + 17 = 0$$

$$x^2 - 8x = -17 \quad \boxed{-4} \text{ (16)}$$

$$x^2 - 8x + 16 = -17 + 16$$

$$(x-4)^2 = -1$$

no solution!

eg4: Solve  $3x^2 + 18x - 24 = 0$

$$x^2 + 6x - 8 = 0$$

$$x^2 + 6x = 8 \quad \boxed{+3} \text{ (9)}$$

$$x^2 + 6x + 9 = 8 + 9$$

$$\sqrt{(x+3)^2} = \sqrt{17}$$

$$x+3 = \pm \sqrt{17}$$

$$\boxed{x = \pm \sqrt{17} - 3}$$

eg5: Solve  $5x^2 + 10x - 4 = 0$

$$5x^2 + 10x = 4 \quad \boxed{+1} \text{ (1)}$$

$$5(x^2 + 2x) = 4$$

$$5(x^2 + 2x + 1) = 4 + 5$$

$$5(x+1)^2 = 9$$

$$\sqrt{(x+1)^2} = \sqrt{\frac{9}{5}}$$

$$x+1 = \pm \frac{3}{\sqrt{5}} \cdot \frac{\sqrt{5}}{\sqrt{5}}$$

$$x = \pm \frac{3\sqrt{5}}{5} - 1$$

$$\boxed{= \frac{\pm 3\sqrt{5} - 5}{5}}$$

eg 6: Solve  $2x^2 - 5x - 1 = 0$

To halve a fraction:

\* double the denom.  
\* reduce

$$2x^2 - 5x = 1$$

$$\boxed{-\frac{5}{4}} \quad \textcircled{\frac{25}{16}}$$

$$2\left(x^2 - \frac{5}{2}x\right) = 1$$

$$2\left(x^2 - \frac{5}{2}x + \frac{25}{16}\right) = 1 + \frac{50}{16}$$

$$2\left(x - \frac{5}{4}\right)^2 = \frac{66}{16}$$

$$\left(x - \frac{5}{4}\right)^2 = \frac{66}{32}$$

$$\sqrt{\left(x - \frac{5}{4}\right)^2} = \sqrt{\frac{33}{16}}$$

$$x - \frac{5}{4} = \frac{\pm\sqrt{33}}{4}$$

$$x = \frac{\pm\sqrt{33} + 5}{4}$$

qs 3-7 p. 274-276



## Ch. 6.3 - The Quadratic Formula

- the **QUADRATIC FORMULA** can be used to find the real roots of quadratic equations.

If  $ax^2 + bx + c = 0$ , then  
( $a \neq 0$ )

$$x = \frac{-b \pm \sqrt{b^2 - 4ac}}{2a}$$

derived by **COMPLETING THE SQUARE** of  $ax^2 + bx + c = 0$

Three possible scenarios:

- all three rely on the value of the DISCRIMINANT  
( $b^2 - 4ac$ ) (RADICAND):

- (i) If  $b^2 - 4ac > 0$ , then two real roots.
- (ii) If  $b^2 - 4ac = 0$ , then one real root.
- (iii) If  $b^2 - 4ac < 0$ , then no real roots.

eg!: Solve  $3x^2 + 5x - 2 = 0$  using the Q.F.

$$a = 3 \quad b = 5 \quad c = -2$$

$$x = \frac{-b \pm \sqrt{b^2 - 4ac}}{2a}$$

$$x = \frac{-5 \pm \sqrt{(5)^2 - 4(3)(-2)}}{2(3)}$$

$$x = \frac{-5 \pm \sqrt{49}}{6}$$

$$x = \frac{-5 \pm 7}{6}$$

$$x = \frac{1}{3}, -2$$

Check!

eq2: Solve  $3x^2 + 2x - 4 = 0$  using the  $\phi.F.$

$$a = 3 \quad b = 2 \quad c = -4$$

$$x = \frac{-b \pm \sqrt{b^2 - 4ac}}{2a}$$

$$x = \frac{-2 \pm \sqrt{(2)^2 - 4(3)(-4)}}{2(3)}$$

$$x = \frac{-2 \pm \sqrt{52}}{6}$$

$$x = \frac{-2 \pm 2\sqrt{13}}{6} = \frac{-2}{6} \pm \frac{2\sqrt{13}}{6} = \boxed{\frac{-1}{3} \pm \frac{\sqrt{13}}{3}}$$

check w/ decimals

eq3: Solve  $9x^2 - 12x + 4 = 0$  using the  $\phi.F.$

$$a = 9 \quad b = -12 \quad c = 4$$

$$x = \frac{-b \pm \sqrt{b^2 - 4ac}}{2a}$$

$$x = \frac{-(-12) \pm \sqrt{(-12)^2 - 4(9)(4)}}{2(9)}$$

$$x = \frac{12 \pm \sqrt{0}}{18} = \frac{12}{18} = \boxed{\frac{2}{3}}$$

eq4: Solve  $2x^2 - 3x + 4 = 0$  using the  $\phi.F.$

$$a = 2, \quad b = -3, \quad c = 4$$

$$x = \frac{-b \pm \sqrt{b^2 - 4ac}}{2a}$$

$$x = \frac{-(-3) \pm \sqrt{(-3)^2 - 4(2)(4)}}{2(2)}$$

$$x = \frac{3 \pm \sqrt{-23}}{4}$$

no solution!

eg5: Solve using the  $\phi$ .F.

$$\frac{2}{x-3} + \frac{3}{x+2} = 1 \quad \text{FIND common denominator.}$$
$$(x-3)(x+2)$$

$$2(x+2) + 3(x-3) = 1(x-3)(x+2)$$

$$2x+4 + 3x-9 = x^2-x-6$$

$$0 = x^2 - 6x - 1$$

$$a = 1 \quad b = -6 \quad c = -1$$

$$x = \frac{-b \pm \sqrt{b^2 - 4ac}}{2a}$$

$$x = \frac{-(-6) \pm \sqrt{(-6)^2 - 4(1)(-1)}}{2(1)}$$

$$x = \frac{6 \pm \sqrt{40}}{2} = \frac{6 \pm 2\sqrt{10}}{2} = \boxed{3 \pm \sqrt{10}}$$

eg6: Solve  
\* derive  $\phi$ .F.?

Hwk: p. 280 - 284 # 1-5, 8.  
(try #7 see eg5 p. 279)

### Chapter 6.5 Word Problem Examples

Eg1: The sum of a number and twice its reciprocal is  $\frac{9}{2}$ . Find the number.

Let  $x =$  the number  
then  $\frac{1}{x} =$  its reciprocal

$$x + 2\left(\frac{1}{x}\right) = \frac{9}{2}$$

$$x\left(x + \frac{2}{x}\right) = \left(\frac{9}{2}\right)x$$

$$2(x^2 + 2) = \left(\frac{9}{2}x\right)2$$

$$2x^2 - 9x + 4 = 0$$

$$(2x^2 - 8x) - (1x + 4) = 0$$

$$2x(x-4) - 1(x-4) = 0$$

$$\rightarrow (x-4)(2x-1) = 0$$

$$\boxed{x = 4, \frac{1}{2}}$$

Eg2: A patrol boat took 2.5 hours for a round trip 12 km up-river and 12 km back down-river. The speed of the current was 2 km/h. What was the speed of the boat in still water?

Let  $x =$  speed of boat in still water

$$d = st \Rightarrow t = \frac{d}{s}$$

$$2.5 = \frac{\text{downriver } 12}{x+2} + \frac{\text{upriver } 12}{x-2}$$

$$2.5(x+2)(x-2) = 12(x-2) + 12(x+2)$$

$$2.5x^2 - 10 = 24x$$

$$5x^2 - 48x - 20 = 0$$

$$5x^2 - 50x + 2x - 20 = 0$$

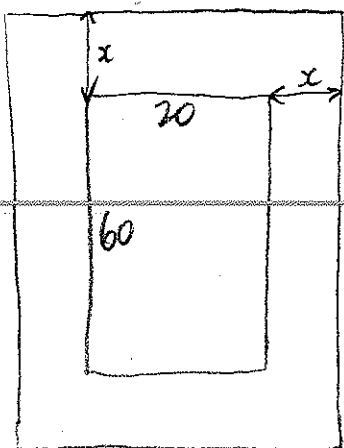
$$5x(x-10) + 2(x-10) = 0$$

$$(x-10)(5x+2) = 0$$

$$\rightarrow \boxed{x = 10},$$
  
$$\boxed{10 \text{ km/h.}}$$

~~$\frac{2}{5}$~~

Eg3: A 20 cm by 60 cm painting has a frame surrounding it. If the frame is the same width all around, and the total area of the frame is 516 cm<sup>2</sup>, then how wide is the frame?



Let  $x$  = width of frame

$$\text{Area}(\text{frame}) = A(\text{big rect.}) - A(\text{painting})$$

$$516 = (60 + 2x)(20 + 2x) - (20)(60)$$

$$516 = 1200 + 160x + 4x^2 - 1200$$

$$0 = 4x^2 + 160x - 516$$

$$0 = x^2 + 40x - 129$$

$$0 = (x + 43)(x - 3)$$

$$x = -43 \quad \boxed{3}$$

Eg4: Sally biked from Mount Douglas to Stelly's, a distance of 25 km, on two consecutive days. On day 1, she rode 3 km/h faster so her ride took 20 minutes less. Calculate her speed on both days and round to the nearest tenth.

Let  $x$  = speed on day 2 (slower speed)  
 then  $x + 3$  = speed on day 1 (faster speed)

$$20 \text{ mins} = \frac{1}{3} \text{ hr.}$$

$$t = \frac{d}{s}$$

$$\frac{1}{3} = \frac{\text{longer time}}{\text{(day 2)}} - \frac{\text{shorter time}}{\text{(day 1)}}$$

$$\frac{1}{3} = \frac{25}{x} - \frac{25}{x+3}$$

$$\frac{1}{3}(x)(x+3) = 25(x+3) - 25x$$

$$\frac{1}{3}x^2 + x = 75$$

$$x^2 + 3x - 225 = 0$$

$$x = \frac{-b \pm \sqrt{b^2 - 4ac}}{2a}$$

$$x = \frac{-3 \pm \sqrt{3^2 - 4(1)(-225)}}{2}$$

$$x = \frac{-3 \pm 30.15}{2} = \boxed{13.6 \text{ km/h}}$$

$$x + 3 = \boxed{16.6 \text{ km/h}}$$

Homework:

p. 294-296 # 1-18

ALSO part 7, 13

p. 270 # 10-15

# Chapter Review

Ch. 4.1-4.2

p. 213-214

# 1-4: omit 2ed/4b/5c

Ch. 6.1-6.3, 6.5

p. 297-299

# 1-6, 8, 10-11 (omit 11)  
through

↓  
only

#

of roots,

not type